

Worksheet 6.3

Full Name: \_\_\_\_\_ Score: \_\_\_\_\_

1. Sketch the region enclosed by the graphs of the given equations. Then, use a definite integral to find the exact value of the volume of the solid obtained by revolving the given region about the given axis of revolution.

(a)  $y = x^2$ ,  $y = 9x$ , about  $x = -1$

(b)  $y = x^2$ ,  $y = 9x$ , about the  $x$ -axis

(c)  $y = x$ ,  $y = x + 2$ ,  $x = 0$ ,  $x = 4$  about the  $x = -3$

(d)  $y = 4x$ ,  $y = 4x^2 - x^3$  about the  $x = -1$

2. Sketch the region enclosed by the graphs of the given equations. Then, use cylindrical shells to **write the definite integral** for the volume of the solid obtained by revolving the given region about the given axis of revolution. Only setup the integral.

(a)  $y = e^x$ ,  $y = 0$ ,  $x = 1$ ,  $x = 2$  about  $x = -2$

(b)  $y = \ln x$ ,  $y = 0$ ,  $x = 2$ , about  $y = -1$

(c)  $y = \frac{1}{\sqrt{x}}$ ,  $y = 0$ ,  $x = 2$ ,  $x = 6$  about the  $y$ -axis

(d)  $y = \frac{\ln x}{\sqrt{x}}$ ,  $y = 0$ ,  $x = 2$ , about the  $y$ -axis