

Worksheet 6.1

Full Name: \_\_\_\_\_ Score: \_\_\_\_\_

1. Sketch the region enclosed by the graphs of the given equations. Then, use a definite integral to find the exact value of the area of the region.

(a)  $y = x^2$ ,  $y = 4x$

(b)  $y = x^3$ ,  $y = 9x$

$$(c) \ y = \frac{1}{x}, \quad y = 0, \quad x = 1, \quad x = e$$

$$(d) \ y = \frac{1}{x^2}, \quad y = 0, \quad x = 1, \quad x = 4$$

(e)  $x = y^2, \quad x = 4$

(f)  $x = e^y, \quad y = 0, \quad x = 1, \quad x = e^2$

$$(g) \quad y = \sin x, \quad y = 0, \quad x = \frac{\pi}{6}, \quad x = \frac{\pi}{2}$$

$$(h) \quad y = \frac{1}{1+x^2}, \quad y = 0, \quad x = \frac{\sqrt{3}}{3}, \quad x = 1$$

(i)  $y = \sqrt{x}$ ,  $y = x^2$ ,  $x = 2$

(j)  $y = \arctan x$ ,  $y = \frac{\pi}{4}$ ,  $y$ -axis