

Name: \_\_\_\_\_

Please read each question carefully to ensure that you are actually answering it. **Show all work.**  
All numerical answers should be left in **exact** form unless otherwise specified.

Page:	1	2	3	4	5	6	Total
Points:	14	18	18	18	14	18	100
Score:							

- 8 1. (a) Find  $\frac{dy}{dx}$  by implicit differentiation.  $2y + \sin x - 2 = x^4 - xy.$

- 6 (b) Find an **equation of the tangent line** to the curve

$$2y + \sin x - 2 = x^4 - xy \quad \text{at the point } (0, 1),$$

in the slope-intercept ( $y = mx + b$ ) form. (Note that it is the same curve in part (a) above.)

12 2. Find the derivatives of the following functions. You do not need to simplify your answer.

(a)  $f(x) = e^{5x} + x^5 + 5^x$

(b)  $f(x) = \ln(x \tan x)$

(c)  $f(x) = \left(\frac{x^3 + 2x}{5x^2 - 3}\right)^7$

6 3. An object is launched vertically up on Planet X. The position,  $s(t)$  (in feet), of the object after  $t$  seconds is given by

$$s(t) = 42t - 6t^2$$

What is the maximum height reached by the object?

- 10 4. Find the linearization  $L(x)$  of the function  $f(x) = \sqrt[3]{x}$  at the number 27, and use it to approximate the value of  $\sqrt[3]{28}$ .

5. Consider the function  $f(x) = 5x^{\frac{1}{3}} - x^{\frac{5}{3}}$ . Answer the following using **calculus**.

- 6 (a) Find the intervals on which  $f$  is increasing or decreasing.

*f is increasing on .....*

*f is decreasing on .....*

- 2 (b) Find the  $x$ -values where  $f$  attains its local maximum and minimum values.

*f has local maximum at  $x = \dots$*

*f has local minimum at  $x = \dots$*

- 8 6. Note that the function  $f(x) = 3x^2 + 2x + 5$  is continuous on  $[-1, 2]$  and differentiable on  $(-1, 2)$  being a polynomial. Find all number(s)  $c$  in  $(-1, 2)$  satisfying the conclusion of the Mean Value Theorem for the function  $f$ .
- 10 7. A girl flies a kite at a height of 600 ft, the wind carrying the kite horizontally away from her at a rate of 12 ft/sec. How fast must she let out the string when the kite is 1000 ft away from her? Assume the string is taut so that it forms a straight line.

- 10 8. Find the absolute maximum and absolute minimum **values** of the function

$$f(x) = x^3 - 3x^2 + 60$$

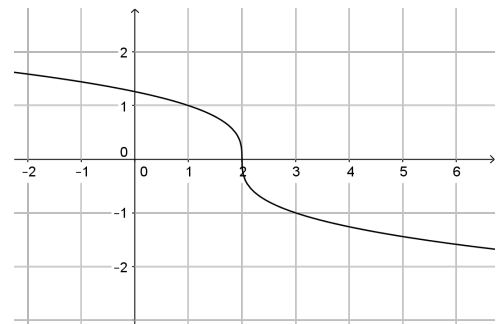
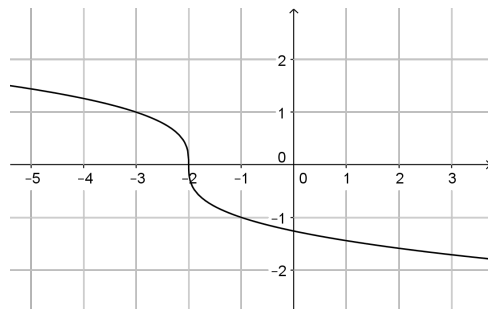
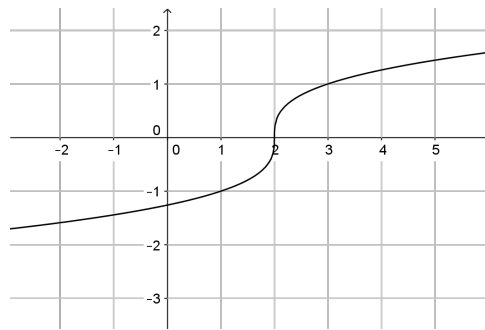
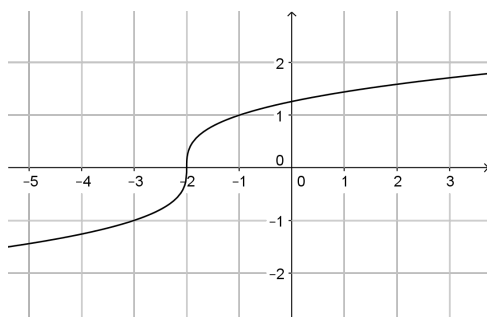
in the interval  $[-3, 1]$ . **Write your answer in the space provided.**

*Absolute max. value: .....*

*Absolute min. value: .....*

- 4 9. Choose a graph of the function  $f$  that is continuous on  $(-\infty, \infty)$  and has the following properties.

$$f'(x) < 0 \text{ and } f''(x) < 0 \text{ on } (-\infty, 2); \quad f'(x) < 0 \text{ and } f''(x) > 0 \text{ on } (2, \infty)$$



- 6 10. Find the **slope** of the tangent line to the curve

$$\tan(xy) = y \quad \text{at the point} \quad \left(\frac{\pi}{4}, 1\right).$$

Circle the correct answer. You do not need to show your work. (No partial credit will be given.)

- 3 11. If  $f(x) = \cos^2 x$ , its derivative,  $f'(x)$ , is given by

(a)  $\frac{\cos^3 x}{3}$       (b)  $-\frac{\sin^3 x}{3}$       (c)  $-\sin^2 x$       (d)  $-2 \cos x \sin x$       (e)  $2 \sin x \cos x$

- 3 12. The derivative of  $y(x) = 3 \log_3(x)$  is given by

(a)  $\frac{3}{x}$       (b)  $\frac{1}{x}$       (c)  $\frac{1}{x \ln 3}$       (d)  $\frac{3}{x \ln 3}$       (e)  $\frac{3}{\ln 3}$

Use the table for the following two questions.

$x$	$f$	$f'$	$g$	$g'$
0	2	-2	2	-1
1	3	10	2	10
2	2	-3	-2	4

- 3 13. If  $H(x) = f(g(x)) + 4$ , find  $H'(0)$ .

(a) 2      (b) 4      (c) 5      (d) 3      (e) -2

- 3 14. If  $J(x) = \tan^{-1}(g(x))$ , find  $J'(1)$ .

(a) 0      (b) 1      (c) 10      (d) 2      (e)  $\frac{1}{10}$