

The Distribution of Sample Means (chap 7)

sampling error = sample mean - true population mean

the standard error of the (sample) mean tells you how much sampling error there is likely to be - so how do you get that?

sampling distribution (of the mean) - a distribution (histogram) of sample means obtained by selecting all possible samples of size n from a population (it's a theoretical thing!)

example: the Pearson fathers data (see reverse for histogram)

mean = 67.687

sd(pop) = 2.745

$N = 1078$

the central limit theorem - gives the properties of the sampling distribution

"For any population with mean μ and standard deviation σ , the distribution of sample means for sample size n will have a mean of μ and a standard deviation of σ/\sqrt{n} and will approach a normal distribution as n approaches infinity."

- * the mean of the sample means will be the same as the mean of the population
- * the standard deviation of the sample means will be the standard deviation of the population divided by the square root of the sample size
- * this number is called the standard error of the mean
- * we usually have to estimate that by using the sample standard deviation
- * as n gets larger (30 or more) the sampling distribution rapidly approaches a normal distribution - this means we can use the z-table to find out what sample means are likely and unlikely
- * if the population is normal to begin with, the sampling distribution will be normal regardless of n
- * in these cases:
 - 68% of the sample means will be within one sem of μ
 - 95% of the sample means will be within two sems of μ
 - > 99% of the sample means will be within three sems of μ

in short, this is the same stuff we did in chapter 6, but using the sem rather than the standard deviation to get z

for an individual raw score: $z = (x - \mu)/sd$

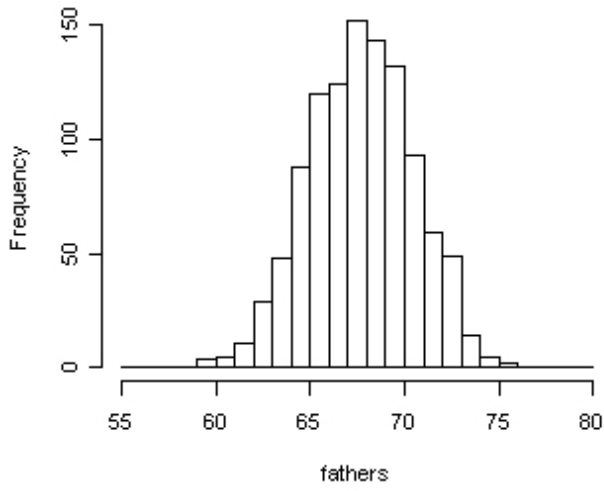
for a sample mean: $z = (\text{mean} - \mu)/\text{sem}$

problems you should look at:

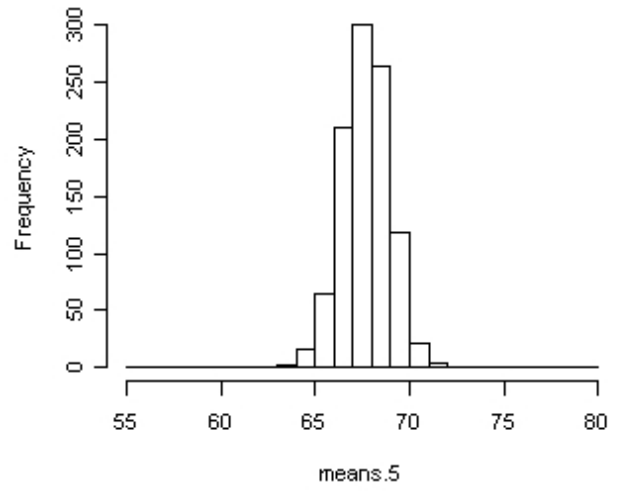
7th ed: 3, 4, 5, 6, 7, 8, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21

6th ed: 2, 4, 5, 6, 8, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23

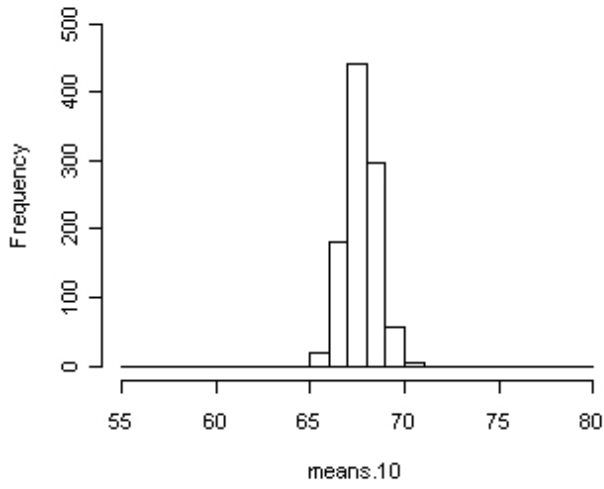
Histogram of fathers



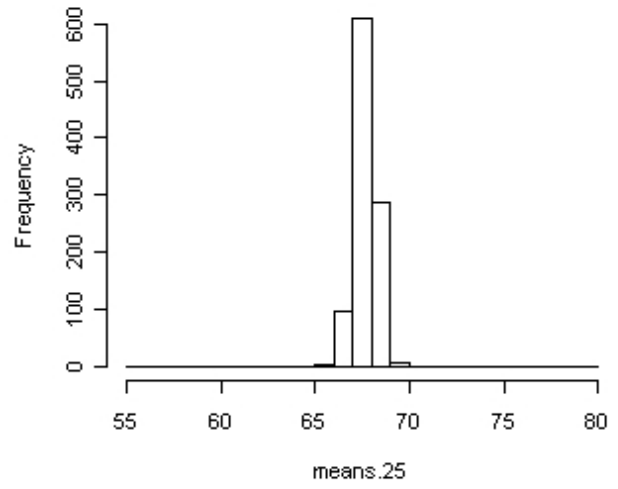
Histogram of means.5



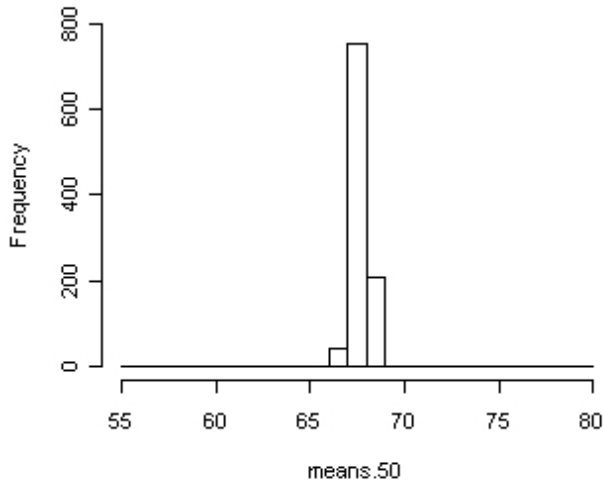
Histogram of means.10



Histogram of means.25



Histogram of means.50



Histogram of means.100

