

MATH 160 Exam 2
CCU Dept. of Math/Stats
Sample A

Name _____

Score _____

1. (a) (10 points) Use implicit differentiation to find $\frac{dy}{dx}$.

$$y^4 - 4y^2 = x^4 - 5x^2$$

- (b) (5 points) Find an equation of the line tangent to the graph of

$$y^4 - 4y^2 = x^4 - 5x^2$$

at the point $(0, -2)$.

2. Compute $\frac{dy}{dx}$ for the following functions.

(a) (10 points) $y = (\cos x)^x$. **(Show work)**.

(b) (10 points) $y = \sqrt[4]{\frac{x^2 + 1}{x^2 - 1}}$.

3. (16 points) If a tank holds 5000 gallons of water, which drains from the bottom of the tank in 40 minutes, then Torricelli's Law gives the volume V of water remaining in the tank after t minutes as

$$V = 5000 \left(1 - \frac{t}{40}\right)^2 \quad 0 \leq t \leq 40$$

- (a) Find the average rate at which water is draining from the tank the first 10 minutes.

- (b) Find the rate at which water is draining from the tank at 10 minutes.

4. (a) (6 points) Given a function $y = f(x)$ and a point $(a, f(a))$ write the equation of the linearization of f at a .

$$L(x) = \underline{\hspace{2cm}}$$

- (b) (10 points) Use a linear approximation to estimate $e^{.025}$. **(Show work)**.

5. (18 points) If a stone thrown vertically upward from the top a 40 ft. building with an initial velocity of 40 ft/s, its height (in feet) after t seconds is $s(t) = 40 + 64t - 16t^2$.

(a) What is the velocity of the stone after t seconds?

(b) What is the maximum height reached by the stone?

(c) What is the velocity of the stone after it has risen 88 feet?

6. (15 points) Choose **one** of the following two related rates problems. You must show all of your work to receive full credit. If you attempt both, **circle** the one that you want to have graded.

- (a) Two cars start moving from the same point. One travels south at 60 mi/h and the other travels west at 25 mi/h. At what rate is the distance between the cars increasing two hours later?
- (b) Water is leaking out of an inverted conical tank at a rate of $10,000 \text{ cm}^3/\text{min}$ at the same time that water is being pumped into the tank at a constant rate. The tank has height 6 meters and the diameter at the top is 4 meters. If the water level is rising at a rate of $20 \text{ cm}/\text{min}$ when the height is 2 meters, find the rate at which water is being pumped into the tank. Note: $V = \frac{1}{3}\pi r^2 h$.